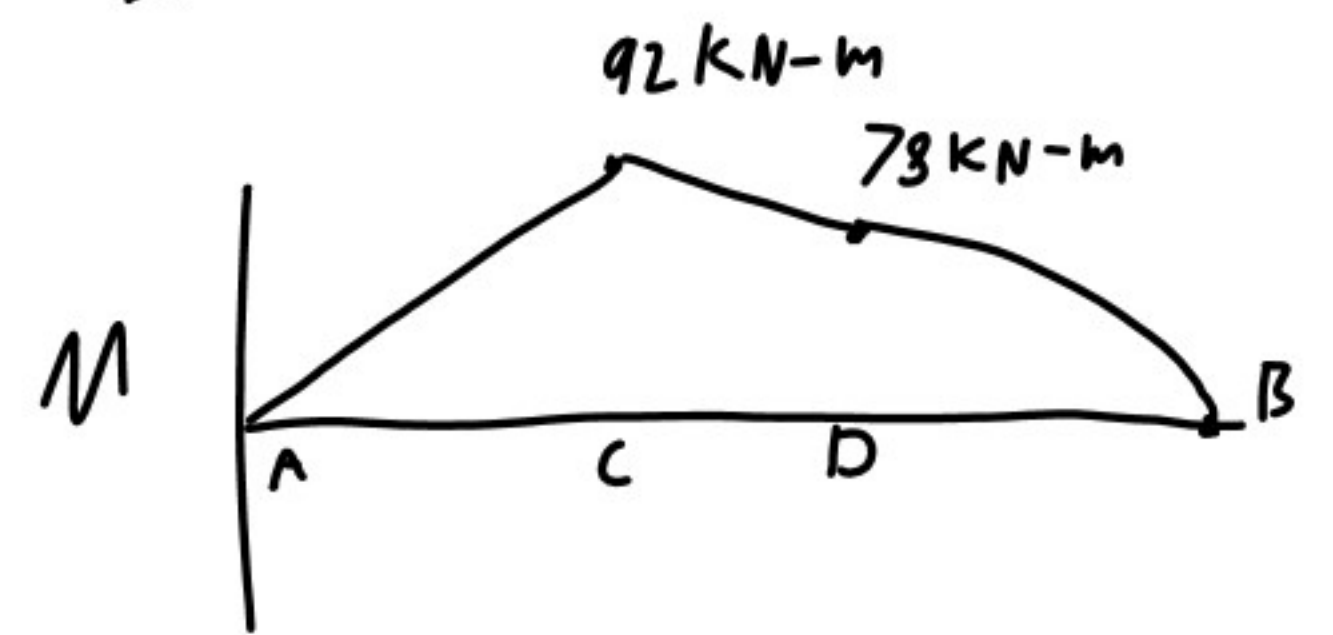
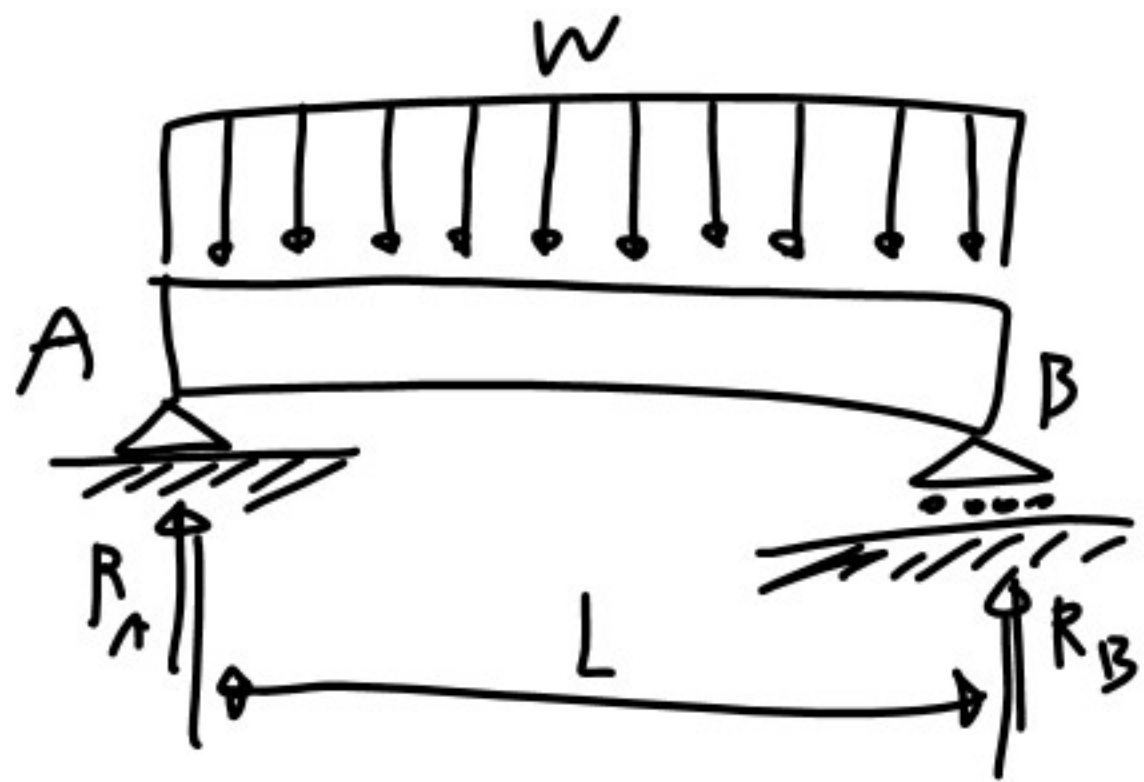


$$\frac{dM}{dx} = V$$





$$\frac{dV}{dx} = -w$$

$$\frac{dM}{dx} = V$$

$$\sum M_A = 0$$

$$LR_B - \frac{L}{2}Lw = 0$$

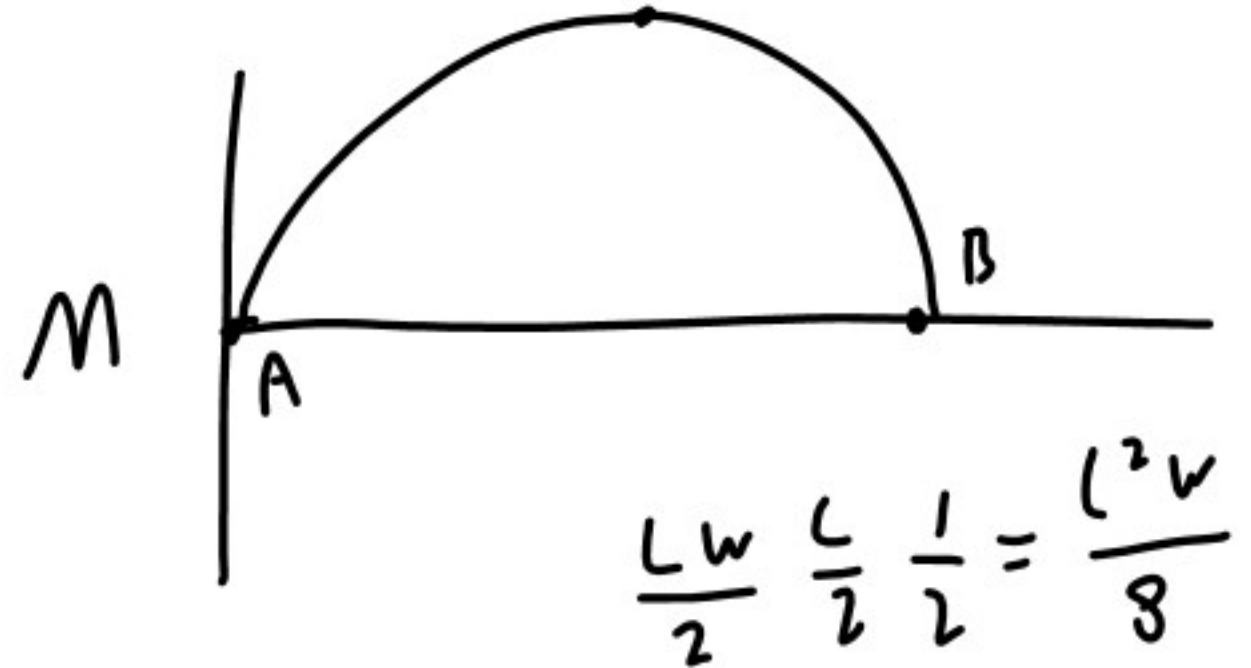
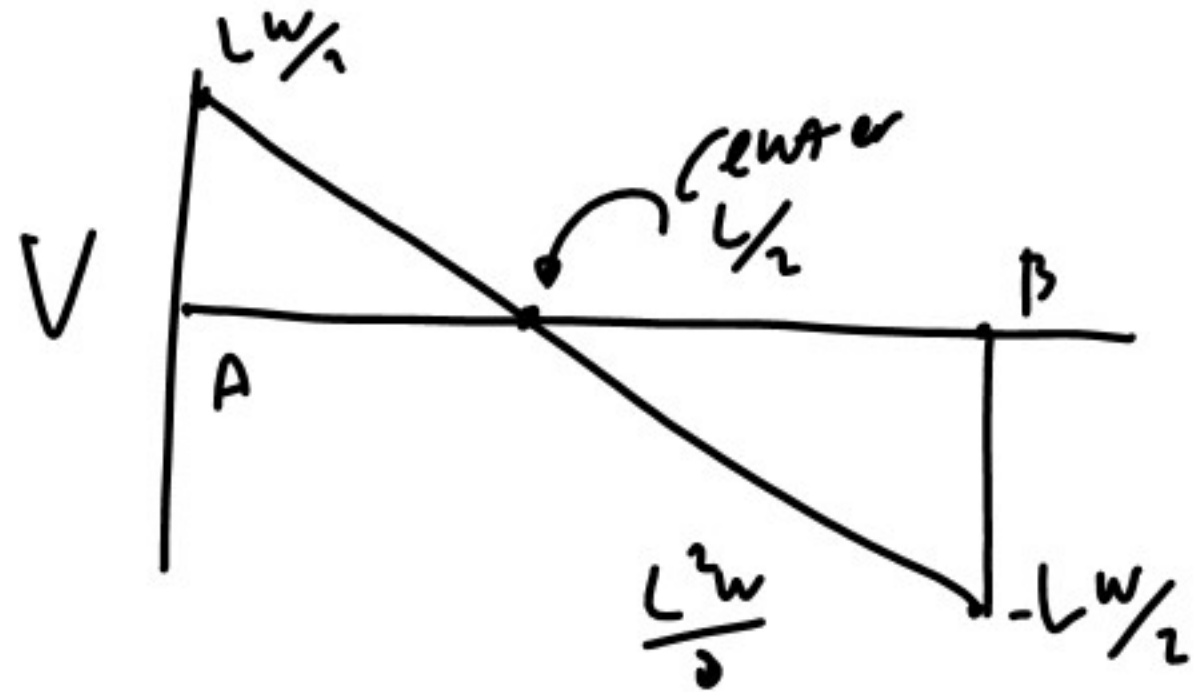
$$LR_B = \frac{L^2w}{2} \quad R_B = \frac{Lw}{2}$$

$$\sum F_y = 0$$

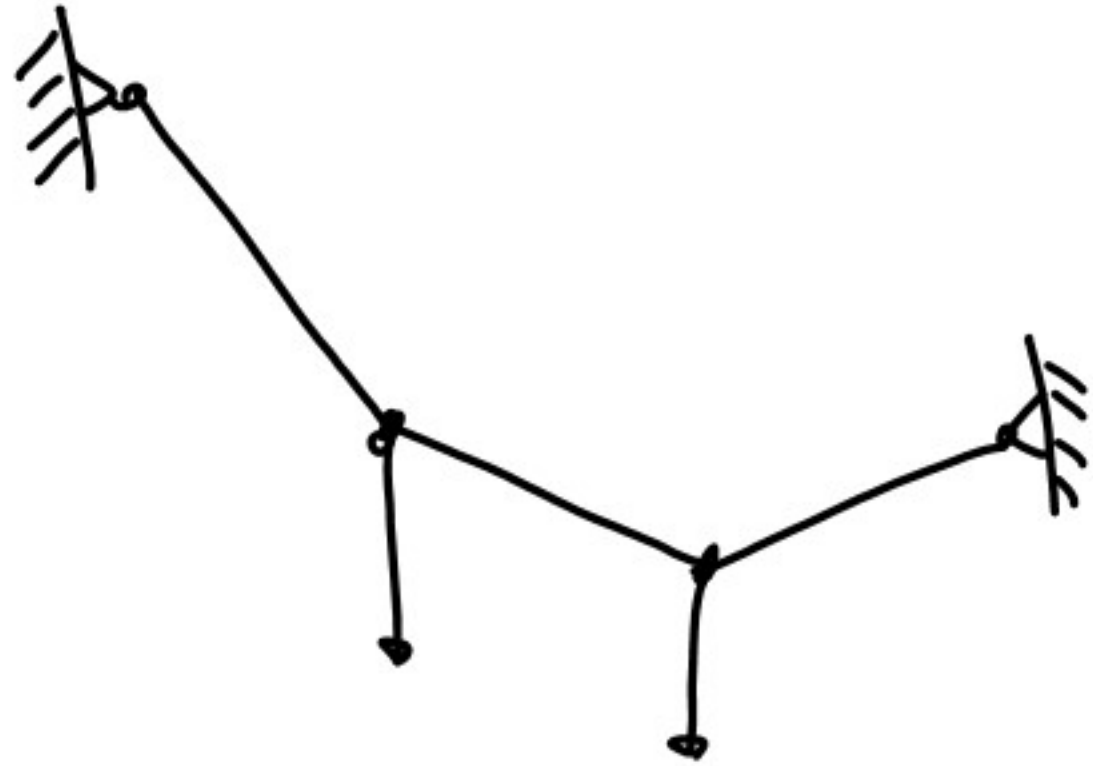
$$R_A + R_B - Lw = 0$$

$$R_A = Lw - R_B = Lw - \frac{Lw}{2}$$

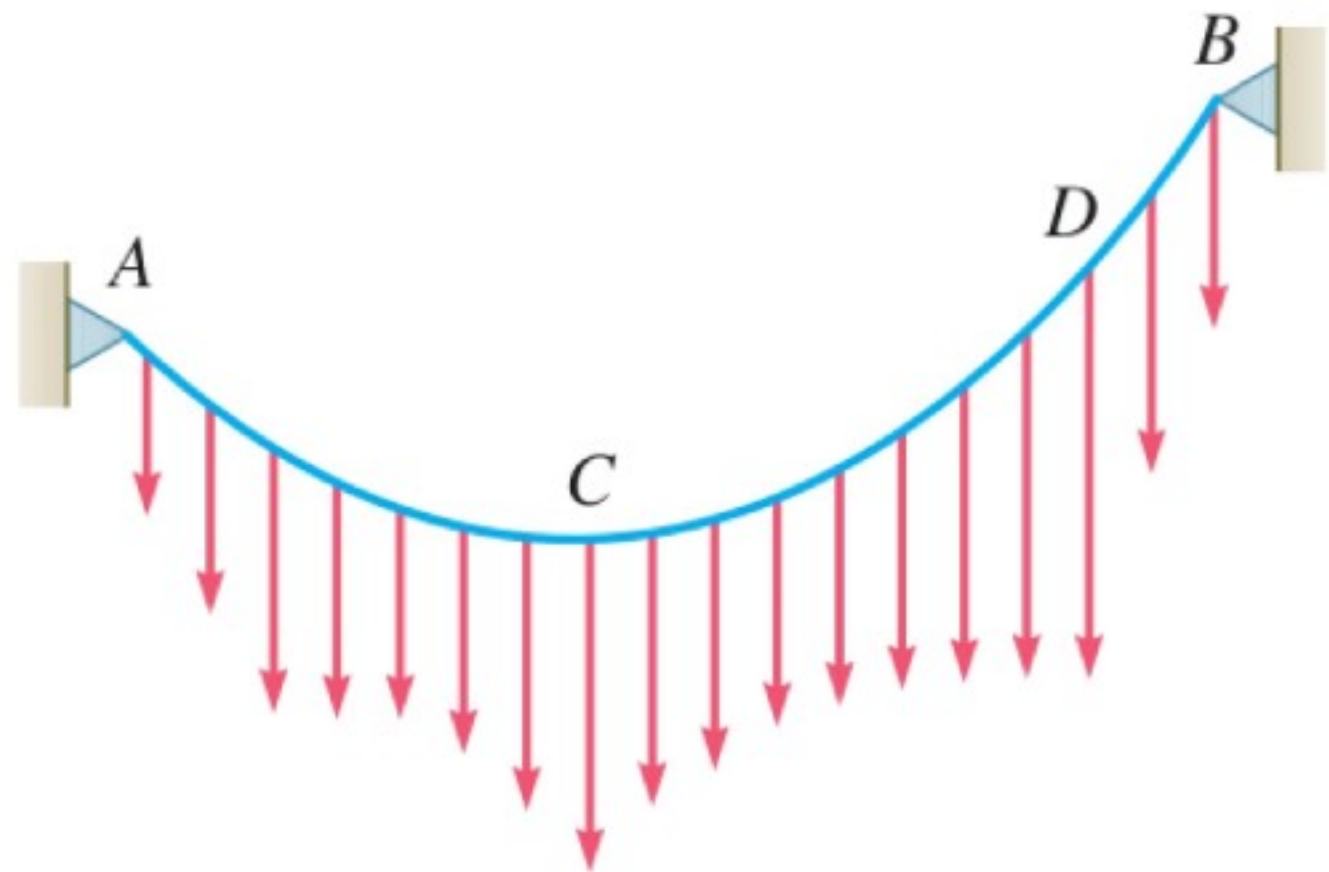
$$R_A = \frac{Lw}{2}$$



Cables



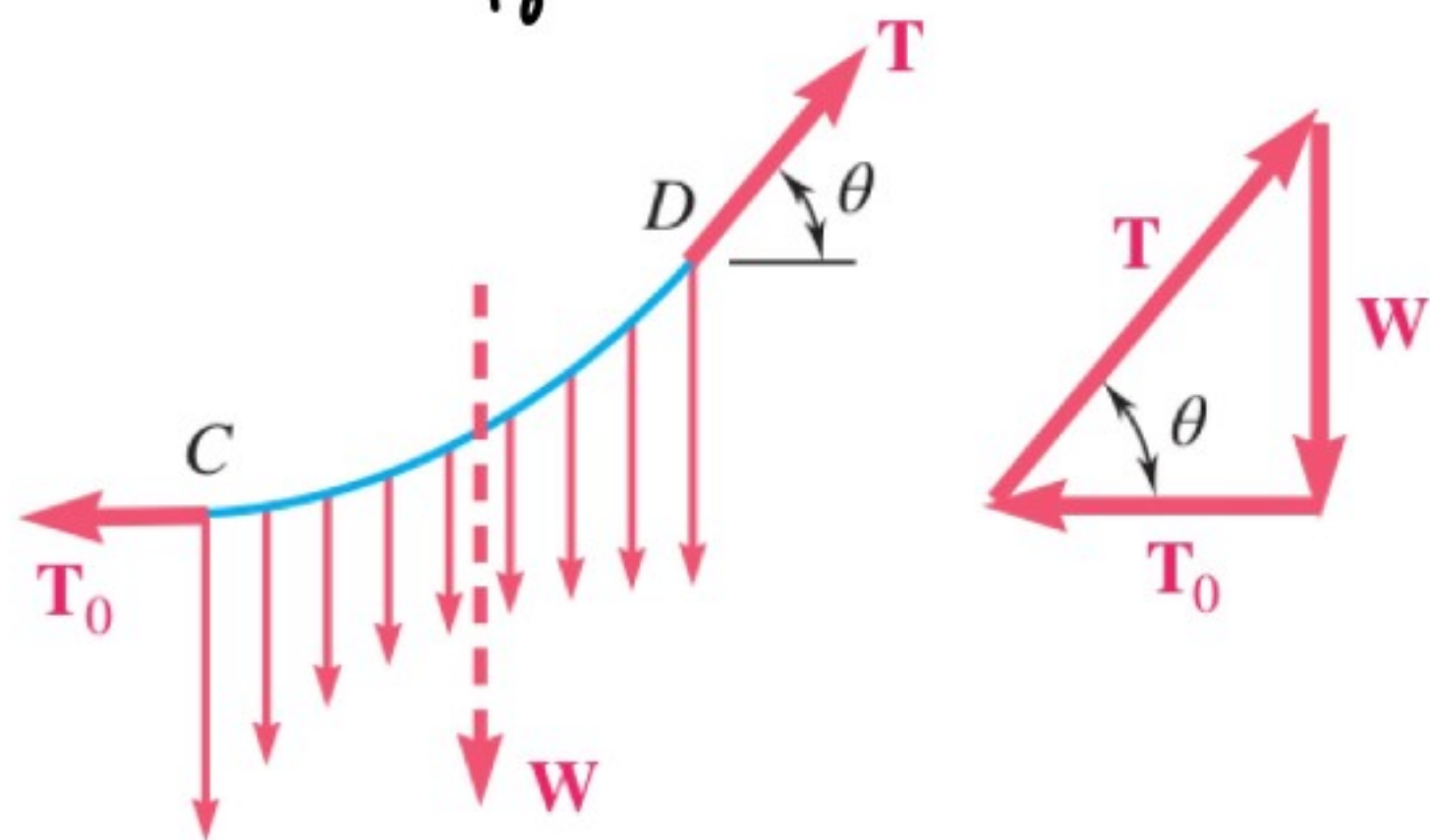
Assume cable massless
Cable inelastic
Cable flexible



$$T \cos \theta = T_0 \quad T \sin \theta = W$$

$$\tan \theta = \frac{W}{T_0}$$

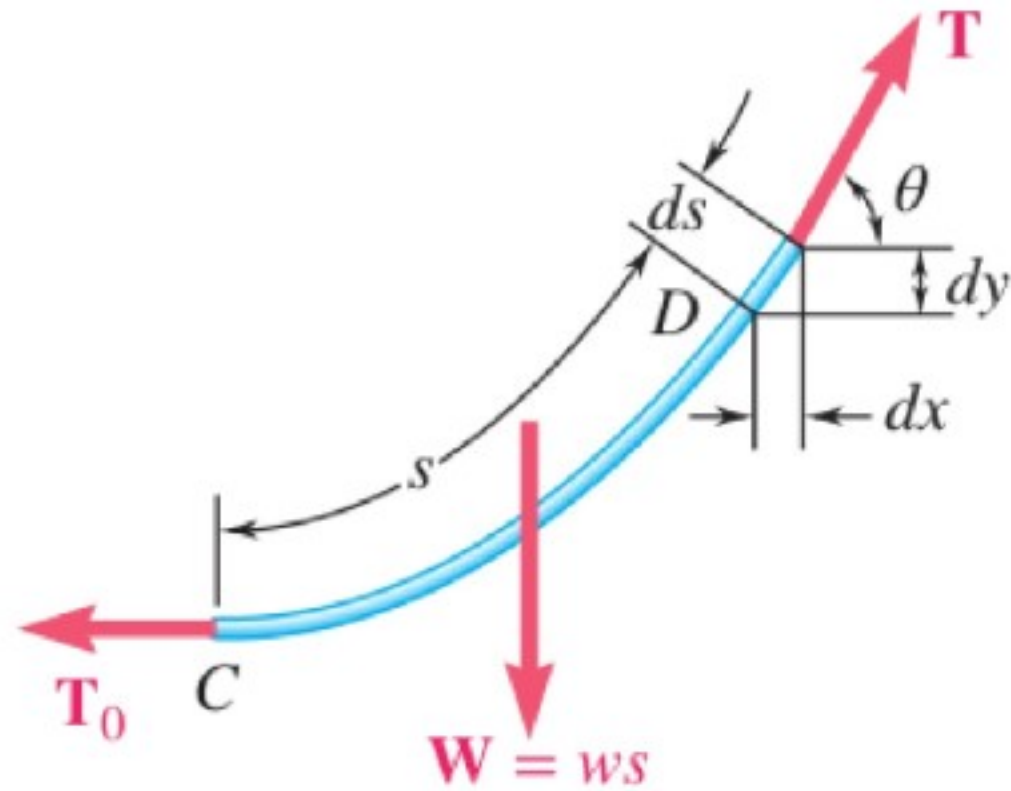
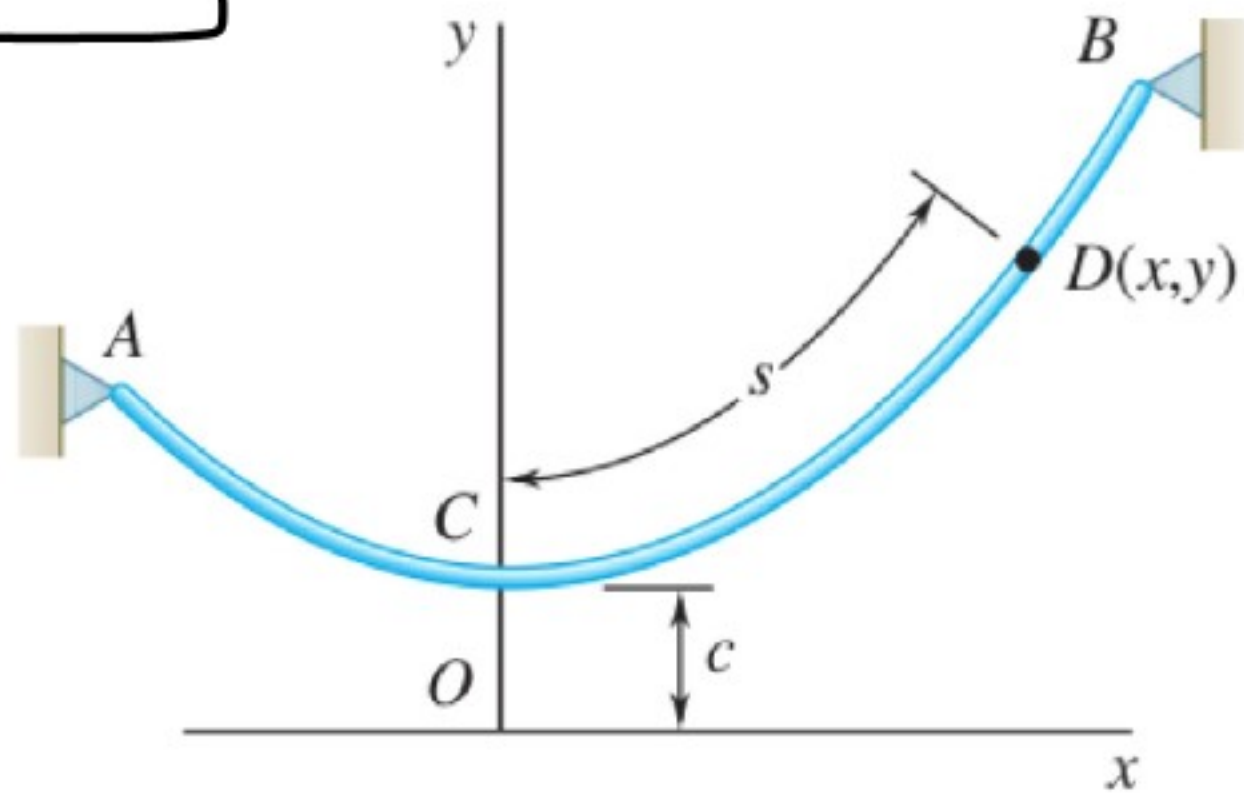
$$T = \sqrt{T_0^2 + W^2}$$



Assume cable has mass

$$C = \frac{T_0}{w}$$

$$T = \sqrt{T_0^2 + w^2 s^2} = \sqrt{C^2 w^2 + w^2 s^2} = w \sqrt{C^2 + s^2}$$



$$dx = ds \cos \theta$$

$$= ds \frac{T_0}{T}$$

$$dx = ds \frac{wC}{w \sqrt{C^2 + s^2}}$$

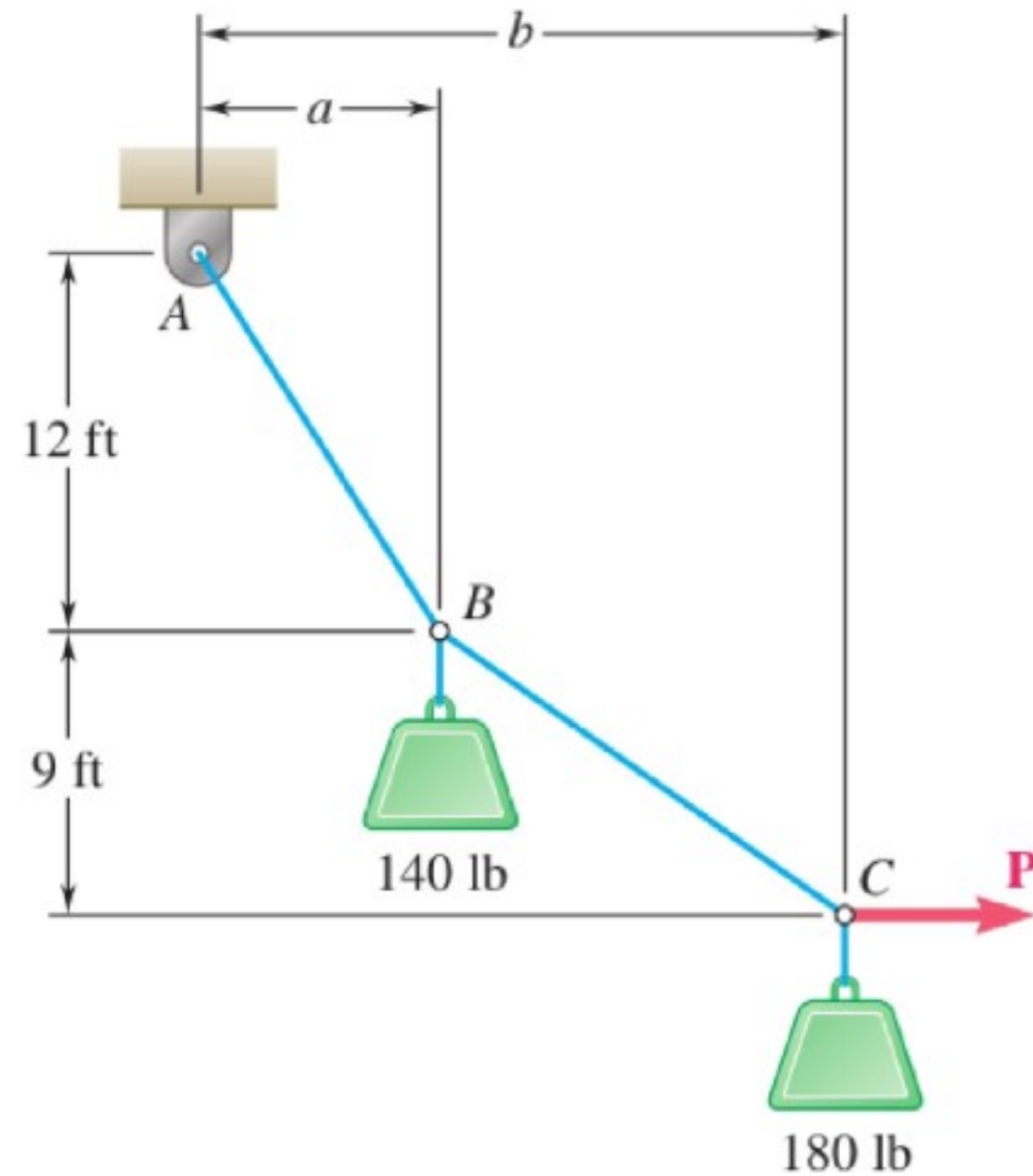
$$\int_0^s dx = \int_0^s \frac{1}{\sqrt{1+s^2/c^2}} ds \quad \Rightarrow \quad s = c \sinh^{-1}\left(\frac{s}{c}\right) \quad \Rightarrow \quad \boxed{s = c \sinh\left(\frac{x}{c}\right)}$$

$$dy = dx \tan \theta = dx \frac{w}{T_0} = dx \frac{ws}{T_0} = dx \frac{s}{c} = dx \frac{c \sinh\left(\frac{x}{c}\right)}{c} = \sinh\left(\frac{x}{c}\right) dx$$

$$y - c = \int_0^x \sinh\left(\frac{x}{c}\right) dx = c \cosh\left(\frac{x}{c}\right) - c \quad \Rightarrow \quad \boxed{y = c \cosh\left(\frac{x}{c}\right)}$$

(catenary)

7.103 Cable ABC supports two loads as shown. Knowing that $b = 21$ ft, determine (a) the required magnitude of the horizontal force \mathbf{P} , (b) the corresponding distance a .



7.104 Cable ABC supports two loads as shown. Determine the distances a and b when a horizontal force \mathbf{P} of magnitude 200 lb is applied at C .

