

**14-2** A steel spur pinion has a diametral pitch of 10 teeth/in, 18 teeth cut full-depth with a  $20^\circ$  pressure angle, and a face width of 1 in. This pinion is expected to transmit 2 hp at a speed of 600 rev/min. Determine the bending stress.

$$\sigma = \frac{K_v W_t P}{F Y} = \frac{1.24 \cdot 233 \text{ lb} \cdot 10 \frac{1}{\text{in}}}{1 \text{ in} \cdot 0.309}$$

$$= 9326 \text{ psi}$$

$$K_v = \frac{1200 + V}{1200} = \frac{1200 + 283}{1200} = 1.24$$

$$P = 10 \text{ teeth/in}$$

$$F = 1 \text{ in}$$

$$Y = 0.309 \quad (\text{Tab 14-2})$$

$$V = r \omega = \frac{d}{2} \omega = \frac{1.8 \text{ in}}{2} \cdot 600 \frac{\text{rev}}{\text{min}} \cdot \frac{2\pi \text{ rad}}{1 \text{ rev}} \cdot \frac{1 \text{ ft}}{12 \text{ in}} = 283 \text{ ft/min}$$

$$d = \frac{N}{P} = \frac{18}{10} = 1.8 \text{ in}$$

$$W_t = \frac{H}{V} = \frac{2 \text{ hp}}{283 \frac{\text{ft}}{\text{min}}} \cdot \frac{33000 \frac{\text{ft} \cdot \text{lb}}{\text{min}}}{1 \text{ hp}} = 233 \text{ lb}$$

**14-6** A  $20^\circ$  full-depth steel spur pinion has 20 teeth and a module of 2 mm and is to transmit 0.5 kW at a speed of 200 rev/min. Find an appropriate face width if the bending stress is not to exceed 75 MPa.

$$m = \frac{d}{N} \quad d = Nm = 20 \cdot 2 \text{ mm} = 40 \text{ mm}$$

$$V = r\omega = \frac{d}{2} \omega = 20 \text{ mm} \cdot 200 \frac{\text{rev}}{\text{min}} \cdot \frac{2\pi \text{ rad}}{1 \text{ rev}} \cdot \frac{1 \text{ min}}{60 \text{ s}} \cdot \frac{1 \text{ m}}{1000 \text{ mm}} = 0.419 \text{ m/s}$$

$$k_v = \frac{6.1 + V}{6.1} = \frac{6.1 + 0.419}{6.1} = 1.07$$

$$Y = 0.322$$

$$W^t = \frac{H}{V} = \frac{500 \text{ W}}{0.419 \text{ m/s}} \cdot \frac{1 \text{ J/s}}{1 \text{ W}} \cdot \frac{1 \text{ Nm}}{1 \text{ J}} = 1193 \text{ N}$$

$$\sigma = \frac{k_v W^t}{F m Y}$$

$$F = \frac{k_v W^t}{\sigma m Y} = \frac{1.07 \cdot 1193 \text{ N}}{75 \text{ MPa} \cdot 2 \text{ mm} \cdot 0.322}$$

$$= 26.4 \frac{\text{N}}{\text{MPa} \cdot \text{mm}} \cdot \frac{1 \text{ MPa}}{1 \times 10^6 \text{ Pa}} \cdot \frac{1 \text{ Pa}}{1 \text{ N/m}^2} \cdot \frac{1000 \text{ mm}}{1 \text{ m}}$$

$$F = 0.0264 \text{ m} = 26.4 \text{ mm}$$