

Mechanical Engineering
345 - Mechatronics
 Midterm Exam 1
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Directions: take-home, all day, open notes, open book. Calculators, MATLAB, etc. allowed. Use your own paper, work neatly, and clearly mark your answers. Partial credit may be given.

Problem bugsul

Write a one- or two-sentence response to each of the following questions and imperatives. The use of equations is acceptable when they appear in a sentence. Don't quote me (use your own words, other than technical terminology).

- a. What is the piecewise linear diode model.
- b. What are the relationships between input and output voltage and current in a transformer? Why?
- c. The current through a capacitor becomes zero. What happens to the voltage across the capacitor?
- d. Explain the how the current from the drain to the source of a MOSFET changes as the gate voltage is varied. Assume the MOSFET is in the saturation region.
- e. When can we use impedance analysis?

$V_2 = N V_1$ $i_2 = -\frac{1}{N} i_1$ $P_1 = P_2$

$\frac{dV_c}{dt} = \frac{1}{C} i_c$ if $i_c = 0$ $\frac{dV_c}{dt} = 0$ $V_c = \text{constant}$

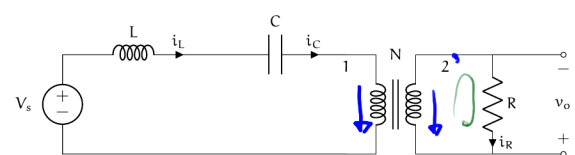
$i_{DS} = k(V_{GS} - V_T)^2$ if V_T is small

$i_{DS} \propto V_{GS}^2$

Problem reorientator

Use the circuit diagram below to answer the following questions and imperatives. Let $V_s = A \sin(\omega t)$. Perform a full circuit analysis, including the transient response to find $v_o(t)$. The initial inductor current is $i_L(0) = 0$ and the initial capacitor voltage $v_c(0) = 0$.

- a. Write the elemental, KCL, and KVL equations.
- b. Write the second-order differential equation for $v_c(t)$ arranged in the standard form.
- c. Convert the initial condition in i_L to a second initial condition in i_c .
- d. Let $R = 10 \text{ k}\Omega$, $L = 100 \text{ mH}$, $C = 100 \text{ }\mu\text{F}$, $N = 5$, $A = 5 \text{ V}$, and $\omega = 500 \text{ rad/s}$ and solve for $v_c(t)$.
- e. Derive an equation to find $v_o(t)$ from $v_c(t)$. This equation will include derivatives of $v_c(t)$. You don't need to add your solution to part d into this equation.



a. Elemental E2's KCL KVL

$V_R = R i_R$ $i_L = i_c = i_1$ $V_s = V_L + V_C + V_1$

$\frac{dV_c}{dt} = \frac{1}{C} i_c$ $i_c = -i_R$ $V_2 = V_R$

$\frac{di_L}{dt} = \frac{1}{L} V_L$

$V_2 = N V_1$
 $i_2 = -\frac{1}{N} i_1$

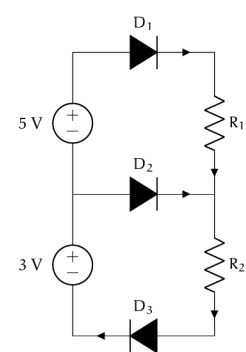
b. $\frac{dV_c}{dt} = \frac{1}{C} i_c = \frac{1}{C} i_L$ $\frac{d^2 V_c}{dt^2} = \frac{1}{C} \frac{di_L}{dt} = \frac{1}{LC} V_L$

$V_2 - V_R = 0$
 $V_2 = V_R$

Problem unrectangularization

Use the circuit diagram below to answer the following questions. Assume $R_1 = R_2$ and that all diodes are ideal.

- a. What state is each diode in?
- b. What is the voltage drop across each of the resistors?



Elemental E2's

$V_{R_1} = R_1 i_{R_1}$
 $V_{R_2} = R_2 i_{R_2}$

KVL

$3 + 5 = V_{D_1} + V_{R_1} + V_{R_2} + V_{D_3}$
 $3 = V_{D_2} + V_{R_2} + V_{D_3}$

KCL

$i_{D_1} = i_{R_1}$
 $i_{R_1} + i_{D_2} = i_{R_2}$
 $i_{R_2} = i_{D_3}$

assume D_1 and D_3 on
 D_2 off

$V_{D_1} = 0$ $i_{D_2} = 0$ $V_{D_3} = 0$

~~$3 = V_{D_2} + V_{R_2} + V_{D_3}$~~

~~$3 - V_{R_1} = V_{D_2}$~~

~~$3 - 9 = V_{D_2}$~~

~~$-1 = V_{D_2} < 0 \checkmark$~~

~~$i_{R_1} + i_{D_2} = i_{R_2}$~~

~~$i_{D_1} = i_{R_1} = i_{R_2} = i_{D_3}$~~

~~$3 = V_{D_1} + V_{R_1} + V_{R_2} + V_{D_3}$~~

$3 = V_{R_1} + V_{R_2}$

$= i_{R_1} R_1 + i_{R_2} R_2$

$= R (i_{R_1} + i_{R_2}) = 2 R i_{R_1}$

if $R \gg 0$ $i_{R_1} > 0$

$i_{D_1} > 0 \checkmark$ $i_{D_3} > 0 \checkmark$

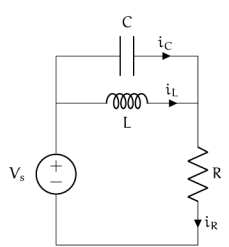
$3 = V_{R_1} + V_{R_2}$

$3 - V_{R_2} = V_{R_1}$

$3 - 9 = \boxed{V_{R_1}}$

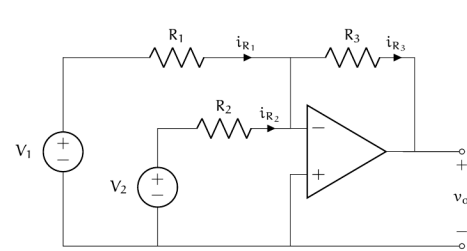
Problem transdimensionism

For the circuit diagram below, perform a circuit analysis to solve for the steady state voltage across the resistor R , $v_R(t)$. Assume $V_s = A e^{j\omega t}$ in sine phasor form and $A \in \mathbb{R}$. Express your answer in sine phasor form.



Problem kirfunkle

Consider the circuit below with two constant voltage sources V_1 and V_2 . Find the steady state voltage output v_o , assuming $R_1 = R_2 = R_3$. Hint: start solving with the equation $v_o = -v_{R_3}$.



c. $i_L(0) = 0$ $i_L = i_c$ $i_c(0) = 0$

$\frac{dV_c}{dt} = \frac{1}{C} i_c$ $\left. \frac{dV_c}{dt} \right|_{t=0} = 0$

e. $V_o = V_R = V_2 = N V_1 = N(V_s - V_L - V_C)$

$= N(V_s - L \frac{di_L}{dt} - V_C)$

$= N(V_s - L \frac{di_c}{dt} - V_C)$

$= N(V_s - LC \frac{d^2 V_c}{dt^2} - V_C)$

$3 = 2 R_2 i_{R_2} = 2 V_{R_2}$

$V_{R_1} = 9$