#### Mechanical Engineering 345 – Mechatronics

345 – Mechatron Midterm Exam 1

Cameron Devine

Directions: take-home, all day, open notes, open book. Calculators, MATLAB, etc. allowed. Use your own paper, work neatly, and clearly mark your answers. Partial credit may be given.

### Problem bupsrul

Write a one- or two-sentence response to each of the following questions and imperatives. The use of equations is acceptable when they appear in a sentence. Don't quote me (use your own words, other than technical terminology).

a What is the piecewise linear diode model.
 b What are the relationships between input and output voltage and current in a transformer? Why?

c The current through a capacitor becomes zero. What happens to the voltage across the capacitor?

**d** Explain the how the current from the drain to the source of a MOSFET changes as the gate voltage is varied. Assume the MOSFET is in the saturation region.

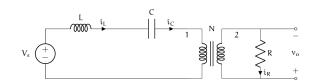
e When can we use impedance analysis?

#### Problem reorientator

Use the circuit diagram below to answer the following questions and imperatives. Let  $V_s = A\sin(\omega t). \mbox{ Perform a full circuit analysis, including the transient response to find $\nu_o(t)$. The initial inductor current is $i_L(0) = 0$ and the initial capacitor voltage $\nu_C(0) = 0$.}$ 

**a** Write the elemental, KCL, and KVL

equations. **b** Write the second-order differential equation for  $v_C(t)$  arranged in the standard form. **c** Convert the initial condition in  $i_L$  to a second initial condition in  $i_C$ . **d** Let  $R=10~k\Omega$ , L=100~mH,  $C=100~\mu F$ , N=5, A=5~V, and  $\omega=500~\frac{rad}{s}$  and solve for  $v_C(t)$ . **e** Derive an equation to find  $v_o(t)$  from  $v_C(t)$ . This equation will include derivatives of  $v_C(t)$ . You don't need to add your solution to part **d** 



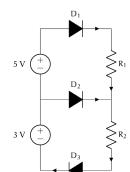
### Problem unrectangularization

into this equation.

Use the circuit diagram below to answer the following questions. Assume  $R_1=R_2$  and that

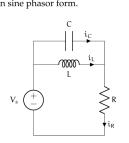
## all diodes are ideal. a What state is each diode in?

**b** What is the voltage drop across each of the resistors?



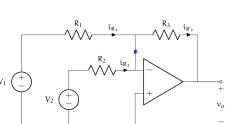
## Problem transidentilationism

For the circuit diagram below, perform a circuit analysis to solve for the steady state voltage across the resister R,  $\nu_R(t)$ . Assume  $V_s = Ae^{j\frac{\pi}{2}}$  in sine phasor form and  $A \in \mathbb{R}$ . Express your answer in sine phasor form.



# Problem kirfunckle

Consider the circuit below with two constant voltage sources  $V_1$  and  $V_2$ . Find the steady state voltage output  $\nu_o$ , assuming  $R_1 = R_2 = R_3$ . Hint: start solving with the equation  $\nu_o = -\nu_{R_3}$ .



$$k \vee l$$
 $V_1 = V_{R_1} + V_{R_3} + V_0$ 
 $V_2 = V_{R_2} + V_{R_3} + V_0$ 
 $V_4 = V_{R_4}$ 
 $V_5 = V_{R_5}$ 

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KCL

$$V_{0} = -V_{R_{3}} = -R_{3} i_{R_{3}}$$

$$= -R_{3} \left( \frac{i_{R_{1}} + i_{R_{1}}}{R_{1}} \right)$$

$$= -R_{3} \left( \frac{V_{R_{1}}}{R_{1}} + \frac{V_{R_{1}}}{R_{2}} \right)$$

$$= -R_{3} \left( \frac{V_{1}}{R_{1}} + \frac{V_{1}}{R_{2}} \right)$$

$$= -\left( V_{1} + V_{2} \right)$$

Elemental Eg's

URI= RziRi

VK3 = K3 iK3

i\_=i-=0

 $V_{R_1} = R_1 i_{R_1}$ 

V = V\_

$$Z_{l} = \frac{1}{jwc}$$

$$Z_{l} = jwc$$

$$V_{R} = V_{s} \frac{R}{\frac{1}{jwc + \frac{1}{jwc}} + R} = V_{s} \frac{jwc}{\frac{jwc}{1 - wcc}} + \frac{1}{1 - wcc}$$

$$V_{s} \frac{R(1 - wcc)}{jwc + R(1 - wcc)} = V_{s} \frac{R - wcc}{jwc} + R - wccc$$

$$= V_{5} \frac{(R - w^{2}RLc)(R - w^{2}RLc - iwL)}{(iwL + R - w^{2}RLc)(R - w^{2}RLc - iwL)}$$

$$= V_{5} \frac{(R - w^{2}RLc)(R - w^{2}RLc - iwL)}{(iwL + R - w^{2}RLc - iwL)}$$

$$= V_{5} \frac{R^{2} - w^{2}R^{2}Lc - iwRL - w^{2}R^{2}Lc + w^{2}L^{2}R^{2}c^{2} + iw^{2}L^{2}}{R^{2} - iw^{2}R^{2}Lc + w^{2}L^{2}R^{2}c^{2} + w^{2}L^{2}}$$

 $Z_e = \frac{1}{\frac{1}{7} + \frac{1}{7}} = \frac{1}{|w_c + \frac{1}{|w_c|}}$ 

$$R_{c}(Z) = \frac{R^{2} - 2 w^{2} R^{2} L^{2} + w^{2} L^{2} R^{2} C^{2}}{R^{2} - 2 w^{2} R^{2} L^{2} + w^{2} L^{2}}$$

$$B = |Z| = \sqrt{R_{c}(2)^{2} + I_{m}(2)^{2}}$$

$$= \frac{\sqrt{(R^{1} - 1 + 1)^{2} R^{2} L_{c} + w^{2} L_{c}^{2} R^{2} c^{2}} + (w^{3} L_{c}^{2} R c - w^{2} R L_{c}^{2})^{2}}{R^{2} - 1 + w^{2} R^{2} L_{c}^{2} + w^{2} L_{c}^{2} R^{2} c^{2} + w^{2} L_{c}^{2}}$$

$$Q = + \epsilon n^{-1} \left(\frac{I_{m}(2)}{R_{c}(2)}\right) = \frac{1}{4} n^{-1} \left(\frac{w^{3} L_{c}^{2} R c - w^{2} L_{c}^{2}}{R^{2} - 1 + w^{2} L_{c}^{2} R^{2} c^{2}}\right)$$

$$V_{R} = V_{S} Z$$

$$= A e^{i \frac{\pi}{2}} Z$$

$$= A e^{i \frac{\pi}{2}} B e^{i \frac{\pi}{2}}$$

$$= A B e^{i \frac{\pi}{2}} (\frac{\pi}{2} + p^{2})$$

$$V_{o} = V_{s} |Z|$$

$$\frac{V_{o}}{V_{s}} = |Z(w)|$$