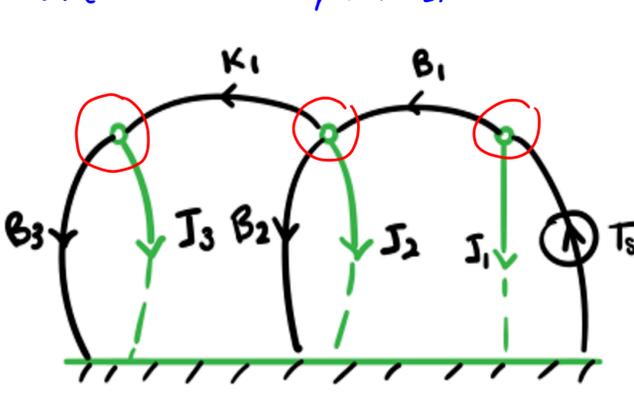


SS, Chunker part 2.



$E = 8$
 $S = 1$
 $S_A = 0$
 $S_T = 1$
 $N = 4$

1. $2E - S = 2(8) - 1 = 15$

a. normal tree ✓

b. primary: $w_{T1}, w_{T2}, w_{T3}, \tau_{B3}, \tau_{K1}, \tau_{B2}, \tau_{B1}, T_s$
 secondary: $\tau_{T1}, \tau_{T2}, \tau_{T3}, w_{B3}, w_{K1}, w_{B2}, w_{B1}, \tau_s$

c. state: $w_{T1}, w_{T2}, w_{T3}, \tau_{K1}$

d.
$$X = \begin{bmatrix} w_{T1} \\ w_{T2} \\ w_{T3} \\ \tau_{K1} \end{bmatrix} \quad u = [T_s] \quad y = \begin{bmatrix} w_{T1} \\ w_{T2} \\ w_{T3} \\ \tau_{B3} \end{bmatrix}$$

e. $E - S = 8 - 1 = 7$

$\tau_{B3} = B_3 w_{B3}$

$\tau_{B2} = B_2 w_{B2}$

$\tau_{B1} = B_1 w_{B1}$

$\frac{dw_{T1}}{dt} = \frac{1}{J_1} \tau_{T1}$

$\frac{dw_{T2}}{dt} = \frac{1}{J_2} \tau_{T2}$

$\frac{dw_{T3}}{dt} = \frac{1}{J_3} \tau_{T3}$

$\frac{d\tau_{K1}}{dt} = K_1 w_{K1}$

f. $N - 1 - S_A = 4 - 1 - 0 = 3$

$\tau_{K1} = \tau_{B3} + \tau_{T3} \Rightarrow \tau_{T3} = \tau_{K1} - \tau_{B3}$

$\tau_{B1} = \tau_{T2} + \tau_{K1} + \tau_{B2} \Rightarrow \tau_{T2} = \tau_{B1} - \tau_{K1} - \tau_{B2}$

$T_s = \tau_{T1} + \tau_{B1} \Rightarrow \tau_{T1} = T_s - \tau_{B1}$

g. $E - N + 1 - S_T = 8 - 4 + 1 - 1 = 4$

$w_{B3} = w_{T3}$

$w_{K1} + w_{T1} - w_{T2} = 0 \Rightarrow w_{K1} = w_{T2} - w_{T1}$

$w_{B2} = w_{T2}$

$w_{B1} + w_{T2} - w_{T1} = 0 \Rightarrow w_{B1} = w_{T1} - w_{T2}$

2. a.

$\tau_{B3} = B_3 w_{T3}$

$\tau_{B2} = B_2 w_{T2}$

$\tau_{B1} = B_1 (w_{T1} - w_{T2})$

$\frac{dw_{T1}}{dt} = \frac{T_s - \tau_{B1}}{J_1}$

$\frac{dw_{T2}}{dt} = \frac{\tau_{B1} - \tau_{K1} - \tau_{B2}}{J_2}$

$\frac{dw_{T3}}{dt} = \frac{\tau_{K1} - \tau_{B3}}{J_3}$

$\frac{d\tau_{K1}}{dt} = K_1 (w_{T2} - w_{T3})$

b.

$\frac{dw_{T1}}{dt} = \frac{T_s - \tau_{B1}}{J_1} = \frac{T_s - B_1 w_{T1} + B_1 w_{T2}}{J_1}$

$\frac{dw_{T2}}{dt} = \frac{\tau_{B1} - \tau_{K1} - \tau_{B2}}{J_2} = \frac{B_1 w_{T1} - B_1 w_{T2} - \tau_{K1} - B_2 w_{T2}}{J_2}$

$\frac{dw_{T3}}{dt} = \frac{\tau_{K1} - \tau_{B3}}{J_3} = \frac{\tau_{K1} - B_3 w_{T3}}{J_3}$

$\frac{d\tau_{K1}}{dt} = K_1 (w_{T2} - w_{T3})$

c.

$$\underbrace{\begin{bmatrix} \dot{w}_{T1} \\ \dot{w}_{T2} \\ \dot{w}_{T3} \\ \dot{\tau}_{K1} \end{bmatrix}}_x = \underbrace{\begin{bmatrix} -B_1/J_1 & B_1/J_1 & 0 & 0 \\ B_1/J_2 & -B_1 - B_2 & 0 & -1/J_2 \\ 0 & 0 & -B_3/J_3 & -1/J_3 \\ 0 & K_1 & -K_1 & 0 \end{bmatrix}}_A \underbrace{\begin{bmatrix} w_{T1} \\ w_{T2} \\ w_{T3} \\ \tau_{K1} \end{bmatrix}}_x + \underbrace{\begin{bmatrix} 1/J_1 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_B [T_s] = u$$

$$\underbrace{\begin{bmatrix} w_{T1} \\ w_{T2} \\ w_{T3} \\ \tau_{B3} \end{bmatrix}}_y = \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & B_3 & 0 \end{bmatrix}}_C \underbrace{\begin{bmatrix} w_{T1} \\ w_{T2} \\ w_{T3} \\ \tau_{K1} \end{bmatrix}}_x + \underbrace{\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}}_D [T_s] = u$$

$\tau_{B3} = B_3 w_{T3}$