

RW 14.8

a) $H(s) = \frac{5s+1}{s+10}$ find Bode plot

$$\begin{aligned} H(j\omega) &= H(s)|_{s \rightarrow j\omega} \\ &= \frac{5j\omega + 1}{j\omega + 10} \cdot \frac{10 - j\omega}{10 - j\omega} = \frac{50j\omega + 5\omega^2 + 10 - j\omega}{100 + \omega^2} \\ &= \frac{10 + 5\omega^2 + 49j\omega}{100 + \omega^2} \end{aligned}$$

$$|H(j\omega)| = \frac{\sqrt{(10 + 5\omega^2)^2 + (49\omega)^2}}{100 + \omega^2}$$

$$= 20 \log_{10} \left(\frac{\sqrt{(10 + 5\omega^2)^2 + (49\omega)^2}}{100 + \omega^2} \right) \text{ dB}$$

$$\angle H(j\omega) = \tan^{-1} \left(\frac{49\omega}{10 + 5\omega^2} \right)$$

| | | | | | |
|----------|-----------|-----------|--------|--------|--------|
| ω | 10^{-2} | 10^{-1} | 10^0 | 10^1 | 10^2 |
| dB | -19 | | | | |
| deg | | | | | |