imp.eqiv Norton and Thévenin theorems

$1\quad \hbox{The following remarkable theorem has been}$ proven.5

Given a linear network of across-variable sources, through-variable sources, and impedances, the behavior at the network's output nodes can be reproduced exactly by a single across-variable source \mathcal{V}_{e} in series with an impedance Z_e .

2 The equivalent linear network has two quantities to determine: V_e and Z_e .

Determining Z_e

3 The equivalent impedance Z_e of a network is equivalent impedance Z_e the impedance between the output nodes with all inputs set to zero. Setting an across-variable source to zero means the across-variable on both its terminals are equal, which is equivalent to treating them as the same node. Setting a through-variable source to zero means the through-variable through it is zero, which is equivalent to treating its nodes as disconnected.

Determining V_e

4 $\;$ The equivalent across-variable source \mathcal{V}_e is $\;$ equivalent across-variable source \mathcal{V}_e the across-variable at the output nodes of the network when they are left open (disconnected from a load). Determining this value typically requires some analysis with the elemental, continuity, and compatibility equations (preferably via impedance methods).

5 Similarly, the following remarkable theorem has been proven.

Theorem imp.2: generalized Norton's theorem

Given a linear network of across-variable sources, through-variable sources, and impedances, the behavior at the network's output nodes can be reproduced exactly by a single through-variable source $\mathcal{F}_{\boldsymbol{e}}$ in parallel with an impedance Z_e .

6 The equivalent network has two quantities to determine: \mathcal{F}_e and Z_e . The equivalent impedance Z_e is identical to that of Thévenin's theorem, which leaves the equivalent through-variable source \mathcal{F}_{e} to be determined.

Determining \mathcal{F}_e

7 The equivalent through-variable source \mathcal{F}_e is —equivalent through-variable source \mathcal{F}_e the through-variable through the output terminals of the network when they are shorted (collapsed to a single node). Determining this value typically requires some analysis with elemental, continuity, and compatibility equations (preferably via impedance methods).

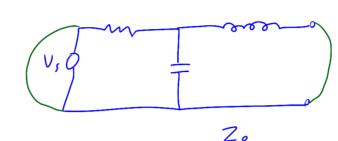
Converting between Thévenin and Norton equivalents

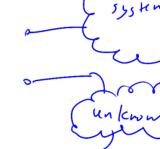
8 There is an equivalence between the two equivalent network models that allows one to convert from one to another with ease. The equivalent impedance Z_ε is identical in each and provides the following equation for converting between the two representations:

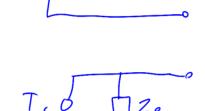
Equation 1 converting between Thévenin and Norton equivalents Ve = Ze Fe

For the circuit

 $5.\$ This lecture is intentionally strongly paralleled in our Electronics lecture on Norton's and Thévenin's theorems.









re: Thévenin and Norton equivalents

