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01.1 Memory
            Computer memory is a collection of bistable
             devices—so they can represent only, say 0 or a 1 \,
             in each bit—organized as bytes: collections of 8
             binary digits or bits. There are 2^8 = 256 unique
             bytes. In more modern systems, each byte (n.b.
             not bit) of memory has a unique address—an
             identifying code. An important aspect of the C
             programming language is that it can deal
             directly with these memory addresses, a
             relatively low-level functionality.
             Memory is not content-specific. It can be used to
             represent numbers (integers, floating point,
             signed numbers, etc.), codes (character codes,
             numeral codes, etc.), and instructions. We must
             keep track of the meaning of its contents. For
             instance, a single bit could represent the state of
             the union: 1 could mean "covfefe" and 0,
             "dumpsterfire." A less exciting example with
             two bits representing four directions:
                    11= north
                    00=300+4
                    ol= east
                   10 = West
             Things you can store in memory
             Pure binary numbers
             Non-negative integers of different magnitudes
             can be stored as pure binary in memory. Here is
             an example using one byte or two nibbles:
                          0000 0000_2 = 0_{10}
                          0000 0001_2 = 1_{10}
                          1111 1110_2 = 254_{10}
                          1111 1111_2 = 255_{10}.
             So the non-negative integers we can store in one
             byte are 0–255, of which there are 2^8 = 256.
             But we can use more than one byte to store a
             non-negative integer in pure binary. If multiple
            bytes are representing a number, the byte that
             occurs first (in terms of address) in memory is
            called the most significant byte (MSB), and the
            byte that occurs last is called the least significant
             byte (LSB). The MSB is usually represented as
             being to the left of the other bytes, and the LSB
             is typically represented as being to the right.
             Here is a list of the total number of possible
             non-negative integers that can be stored in \ensuremath{n}
            bits (formula: 2<sup>n</sup>) for typical values of n:
                          2^8 =
                                           256
                          2^{16} =
                                        65,536
                          2^{24} = 16,777,216
                          2^{32} = 4,294,967,296.
             8-bit two's complement signed binary
             How can a negative number be stored in
             memory? A single byte can store 256 unique
             pieces of information. For decimal numbers,
             this can range 0 to 255 or (say) -128 to 127.
            A very convenient binary representation is
             called two's complement. A number x has two's
             complement in n bits of (2^n - x)_2; that is, the
             number of unique numbers representable minus
             the number, represented in binary. For instance,
                                                             1. The first borrow might seem strange, but it's simply 10_2-01_2=2_{10}-1_{10}=1_{10}=01_2.
             the 8-bit two's complement of 0110 1000 is<sup>1</sup>
                              11111
1000000000
                                                            01101002= 810+37, +64,0=107,0
                               -0110\,1000
                               10011000
                                                            100110002 - 01100111, - 011010002
             Below are listed some 8-bit two's complement
             decimal interpretations of binary numbers.
                           0000 \ 0000_2 = 0
                           0000 \ 0001_2 = 1
                           0111 \ 1111_2 = 127
                           1000 \ 0000_2 = -128
                           1000 0001_2 = -127
                           1111 1110<sub>2</sub> = -2
                          1111 1111_2 = -1
             As if in Pac-Man, starting from the middle and
             exiting screen-right, only to appear
             screen-left—counting "up" loops one back
             down to negative numbers. Note that positive
             two's complements are the same as their pure
             binary counterparts.
             There are two more-convenient ways to find the
             two's complement:
               1. switching all bits (0 \mapsto 1 and 1 \mapsto 0), then
                  adding 1 or
               2. starting from the right, copying all bits
                  through the first 1 encountered, then
                  switching all thereafter.
             Both methods can be seen to always hold from
             the subtraction definition.
             The two's complement of the two's complement
            of x is x; that is, it is its own inverse.
            Example 01.1 -1
                                                              re: two's complement
            Find the two's complement of 0000 0101.
             1111 1010 - 1111 1011
             If a binary number is interpreted as a two's
             complement binary number, it is negative if its
             most significant bit (msbit) is 1.
             Binary coded decimal (BCD)
             A binary coded decimal (BCD) represents each
             decimal digit with a nibble, so a series of nibbles
                                                                     nibble 4 biss 29=16
             can represent a decimal number. This leads to
             slightly less-dense storage, but is still useful for
             high-precision computation.
            Example 01.1 -2
                                                              re: BCD for rounding error
            Recall that the number 421.73 had an infinitely
             long binary representation in Example 00.4 -
             1. Represent this number in BCD. Let there be
             an "implied" decimal point, as some encodings
             define, between the third and fourth nibbles.
                       0100
                       0010
                       0001
                      0111
                      0011
                 BCD: 0100 0010 0001 0111 0011
             Floating point
             Floating point numbers can represent very large
             or very small numbers with limited space. It is
             for computer memory what scientific notation is
             for a small piece of paper: that is, it represents a
             number as a \underline{\text{mantissa}}^2 x and an \underline{\text{exponent }} n; 2. The mantissa is also called the significant or coefficient.
             that is, x2^n, where we have used the
            conventional base of 2.
             Consider the following illustration of a 32-bit
             (four-byte) floating point representation.
             We would interpret this as, for instance,
                         .1011... × 2 1011 0110
                       24-bit mantissa 8-bit exponent
            Character codes
             In addition to numbers, memory can store
            character codes: encoded alphabetic, special
             symbols, emojis, etc.
             The most common character code is the
            American Standard Code for Information
            Interchange (ASCII). It's a 7-bit code, so there
are 128 unique character codes.
             It leaves the eighth bit of a byte, "bit seven," the
             parity bit, to be checked for transmission errors.
             It works as follows. Set (1) or reset (0) before
             transmission such that the total number of set
            (1) bits is either even or odd. If the system is
             using even parity, an even number of bits are
             set; or if it's using odd parity, an odd number of
            bits are set.
            For instance, under odd parity, if the byte 1100
            1101 is sent and the byte 1100 0101 is received,
             with its even number of set bits, the receiving
             system knows there has been a transmission
             error.
             Instructions
             Instructions are codes that direct the operation
             of a microprocessor. The myRIO has an ARM
            Cortex-A9 processor with 32-bit instructions.
            Example 01.1 -3
                                                              re: memory interpretation
             Suppose the following is stored in a byte of
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D 416 12 13 14 15 DEF Each byte is given a unique positive integer address distinct from its contents. 30010 = 00000001 0010 1100 address contents 0000 0001 0010 1100 When storing a multi-byte number, we use the bigendian convention: the MSB is stored at the lower address. The littleendian convention

1101 01012 = 12810+6910+910+10= 21310 unsigned in+

1101 01012 - 001010102 - 001010112 = 110+ 210 +810+3210 = 4310 =-4310 8 bit signed le complement

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B

memory: 1101 0101 or D5. How might this be

1101, = 16 0101, = 516 = 510

In memory, bits are grouped into bytes of eight bits. Each byte is often considered as two nibbles, the contents of each represented by a hexadecimal numeral. For instance, a byte

1101 0101=101 instruction

might be represented as follows.

1101 0100,

stores the MSB at the higher address.

interpreted?

Memory organization