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Objectives
The objectives of this exercise are to:
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**06.L** Lab Exercise: Transfer function generator

1. Use real-time clock interrupts to provide

(2.) Implement an arbitrary transfer function

generator. (3.) Introduce A/D and D/A conversion. Introduction

In this lab exercise, you will write a general

purpose program capable of approximating the performance of any SISO, LTI system! The system input and output will both be analog electrical signals. Your program will implement this with a difference equation. At the beginning of each BTI, your ISR will read an analog input to obtain the current input value, compute the current value of the output y(n), and apply the current output value to an analog output. This process continues until ← is entered on

the keypad. The input voltage will be provided by a function generator. Both the input and output voltages will be displayed on the oscilloscope. You will use three new myRIO features in this experiment: an interrupt timer, the ADC, and the DAC. The first is described in detail in Resource 12 and the others in Resource 14.

Although we could implement the differen equation Eq. 4 as shown, the sensitivity of the output to the coefficients leads to numerical inaccuracies as the order of the system N becomes large, so we use the biquad cascade representation of Lec. 06.4.

## The program consists of a main function and an

Pre-laboratory preparation

interrupt service routine (ISR) running in a separate thread. The ISR is set to execute with a period of 0.5 ms (determined by the Timer IRQ), and computes the DAC output from the ADC input by means of a difference equation. Main program

1. Set up and enable the Timer IRQ interrupt, 2. Enter a loop, ending only when a  $\leftarrow$  is

terminate.

received from the keypad. Use getkey. 3. Signal the timer thread to terminate using the irqThreadRdy flag, and wait for it to

The only tasks of main will be the following.

Interrupt service routine The interrupt service routine thread implements a dynamic system. The heart of the ISR is a while loop that checks the irqThreadRdy flag (set in main) to see if the thread should continue. Before the loop begins, initialize the analog input/output, and set the analog output to 0 V. Each time through the loop:

1. Get ready for the next interrupt by waiting for the IRQ to assert. Then write the time interval to wait between interrupts (BTI) to the IRQTIMERWRITE register and write TRUE to the IRQTIMERSETTIME register. 2. Read the analog input to obtain the current input value x(n). 3. Call a function cascade (see below) to

calculate the current value of the output y(n) by computing all of the sections in the biquad cascade. Each biquad section is computed according to Eq. 1. 4. Send the output value to the analog output.
5. Acknowledge the interrupt.

arrays associated with the discrete dynamic system, including: 1. the length of the BTI in microseconds, 2. the number of biquad sections  $n_s$ , and 3. the system constants  $(a_i \text{ and } b_i)$  for the biquad sections.

The dynamic system corresponding to the collection of biquad sections can be

After the loop terminates, save the response to

The ISR must allocate storage for variables and

Lab6.mat.

conveniently referred to and manipulated by first defining a structure to contain the coefficients and previous values of input and output for a single biquad section. We might define a "biquad" structure as follows. double b0; double b1; double b2; // numerator double a0; double a1; double a2; // denominator double x0; double x1; double x2; // input

double y1; double y2; This definition should be placed just before the prototypes section of your program. Then, a specific dynamic system can be defined

as an array of these biquad structures, each array element corresponds to an individual

biquad section:

int myFilter\_ns = 2; // No. of sections uint32\_t timeoutValue = 500; // T - us; f\_s = 2000 E static struct biquad myFilter[] = { {1.0000e+00, 9.9999e-01, 0.0000e+00, 1.0000e+00, -8.8177e-01, 0.0000e+00, 0, 0, 0, 0, 0} {2.1878e-04, 4.3755e-04, 2.1878e-04, 1.0000e+00, -1.8674e+00, 8.8220e-01, 0, 0, 0, 0, 0 This system description can be placed within the ISR, near its beginning. The first two lines

establish the number of biquad sections, and the length of the BTI in microseconds. Finally,

myFilter is the name of an array of biquad structures being initialized. For testing purposes, the initialized constants in the example above correspond to a system of two biquad sections ( $n_s = 2$ ), encoding a unity-gain low-pass filter, with sampling frequency of 2000 Hz. Derived using Tustin's method, they correspond to a third-order continuous system having a pair of complex poles with natural frequency of 40 Hz, and with damping ratio 0.5. The remaining real pole is at 40 Hz. Crazy about pointers! The most challenging part of this task is the calculation of the current output value y(n). The use of pointers makes the calculation both

Don't be tempted to code this algorithm using array indices (instead of pointers); that would be much too slow for our purposes.

straightforward and efficient. Box 06.1 hint

The cascade function The cascade function implements the complete

dynamic system by passing the measured input through the string of biquad sections. The ISR must pass to cascade the value of the current input x(n) measured by the ADC, the number of

biquad sections  $n_s$ , the array of biquad structures containing the coefficients and history variables  $(x_{\mathfrak{i}} \text{ and } y_{\mathfrak{i}})$  for all sections. It might have a prototype that looks like: double cascade( double xin, struct biquad \*fa,  $\ensuremath{//}\xspace$  biquad array double ymin,

corresponding number of biquad sections, and ymin and ymax are the saturation limits. In the above example, myFilter would be passed through fa. The value returned by cascade is the current value of the system output y(n). Coding cacade An efficient way to code cascade is to allocate a

Here, xin is the current system input, fa is the name of an array of biquad structures, ns is the

pointer f in cascade that will be used to point to elements of the array of biquad structures. Begin the function by equating the pointer to the

double ymax

first element in the array (i.e. the first biquad): f = fa;. Variables inside the biquad structure are accessed by using the pointer name, e. g. f->a0, f->b0, f->x0, f->y1, etc. (The ->operator is equivalent to dereferencing and then accessing a member (say, (\*f).a0) and is typed as a minus sign immediately followed by >.) Then, loop  $n_s$  times, to cycle through each of the biquad sections in the array. At the beginning of each loop, the output value y0 of previous biquad must be passed to the input value f->x0 of the current biquad. Within the loop, coding the output value y0 might look like: f->b0\*f->x0 + f->b1\*f->x1 + // ... etc.

)/f->a0; See Equation 1. Each time through the loop, after the output value has been computed, the previous values x and y must be updated, so that they will be correct at the next time step. For example,

incremented to advance to the next biquad in the array. One more point: if the DAC is given a value beyond its range [-10, +10] V, it will saturate its output value appropriately. However, our difference equation Eq. 1 depends on previous values of the output, but doesn't saturate. To

f->x2 = f->x1; f->x1 = f->x0; // ... etc.

At the end of the loop, the pointer f is

correct this disparity, cascade should saturate the output y0 of the final biquad before it is saved for the next iteration. For example, define the macro #define SATURATE(x,lo,hi) { \  $((x) < (lo) ? (lo) : (x) > (hi) ? (hi) : (x)) \setminus$ 

Pass appropriate values of the xmin and xmax parameters to cascade. Then, for the last

biquad, immediately after y0 is computed, saturate its value: y0 = SATURATE(y0, ymin, ymax);

Laboratory Procedure A good strategy to follow in writing this program is to first implement and debug everything except the calculation of the biquad cascade. That is, set up the main program and the ISR, including all arrays and timing. In the

ISR, simply pass the input value from the ADC directly to the DAC. For example, VADin = Aio\_Read(&CIO);

Aio\_Write(&COO, VADin); This will allow you to observe the input and output on the oscilloscope, and determine if the interrupt timing is functioning properly. When you have debugged those portions of the program augment the code above with the call

to cascade. Does it work?

The low-pass digital filter described above was derived using Tustin's method from the transfer function of the three-pole continuous system:  $V_{out}(s)$  $=\frac{1}{(s+\omega_n)(s^2+2\zeta\omega_n s+\omega_n^2)}$  $V_{in}(s)$ 

where  $\omega_n = 2\pi \times 40 \text{ rad/s}$ , and  $\zeta = 0.5$ . This system belongs to a class of filters called Butterworth filters. They are signal processing

Step response Using the oscilloscope (DC coupled), observe the step response of the system by applying a low frequency square wave (e.g. at 8 Hz) with an amplitude of  $\underline{5}\ V$  as the input with the function generator. Save the input and output of cascade in

filters designed to have the flattest possible frequency response in the passband.

500-point buffers. After the timer loop ends, save the buffers to  ${\tt Lab6.mat},$  and transfer the data to Matlab. Plot and compare the measured

step response to the theoretical response of the corresponding continuous system.<sup>6</sup>. Explain. Frequency response Again, using the oscilloscope (AC coupled), observe the frequency response by altering the frequency of a 5 V input sine wave. Record (write down) the amplitude and phase of the output relative to the input sine wave at the following frequencies: [5, 10, 20, 40, 60, 100, 140, 200] Hz. Given the input amplitude, compute the transfer function magnitude (dB) at each frequency.

In Matlab, plot the theoretical magnitude (dB) and phase (deg) versus the frequency (Hz on a logarithmic scale) for the continuous system

transfer function.<sup>7</sup> Plot the corresponding

theoretical frequency response. Explain.

measured data as discrete symbols on top of the

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7. To generate the data for this plot, Matlab's bode is a good choice. Note

that the specifications for the plot format require you to generate the plot separately from your call to bode.

6. To simulate the theoretical response, Matlab's lsim is a good choice.