

9.2

17-20 WORK

Find the work done by a force \mathbf{p} acting on a body if the body is displaced along the straight segment \overline{AB} from A to B . Sketch \overline{AB} and \mathbf{p} . Show the details.

17. $\mathbf{p} = [2, 5, 0]$, $A: (1, 3, 3)$, $B: (3, 5, 5)$

18. $\mathbf{p} = [-1, -2, 4]$, $A: (0, 0, 0)$, $B: (6, 7, 5)$

19. $\mathbf{p} = [0, 4, 3]$, $A: (4, 5, -1)$, $B: (1, 3, 0)$

20. $\mathbf{p} = [6, -3, -3]$, $A: (1, 5, 2)$, $B: (3, 4, 1)$

21. **Resultant.** Is the work done by the resultant of two forces in a displacement the sum of the work done by each of the forces separately? Give proof or counterexample.

$$\text{force } \mathbf{p} = \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix}$$

$$\overline{AB} = B - A$$

$$= \begin{bmatrix} 3 \\ 5 \\ 5 \end{bmatrix} - \begin{bmatrix} 1 \\ 3 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ 2 \end{bmatrix}$$

$$W = F \cdot d$$

$$= \mathbf{p} \cdot \overline{AB}$$

$$= \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix} \cdot \begin{bmatrix} 2 \\ 2 \\ 2 \end{bmatrix} = 2 \cdot 2 + 5 \cdot 2 + 0 \cdot 2$$

$$= 4 + 10 + 0 = 14$$