

9.8.2

$$v = [0, \cos(xyz), \sin(xyz)]$$

$$\operatorname{div}(v) = \frac{\partial v_1}{\partial x} + \frac{\partial v_2}{\partial y} + \frac{\partial v_3}{\partial z}$$

$$= 0 - xz \sin(xyz) + xy \cos(xyz)$$

$$f: \mathbb{R}^n \rightarrow \mathbb{R}$$

$$\operatorname{div}(\nabla f) =$$

$$= \frac{\partial}{\partial x} \nabla f_1 + \frac{\partial}{\partial y} \nabla f_2 + \dots$$

$$= \frac{\partial}{\partial x} \frac{\partial}{\partial x} f + \frac{\partial}{\partial y} \frac{\partial}{\partial y} f + \dots$$

$$\frac{\partial}{\partial t} u = \alpha \operatorname{div}(\nabla u) \quad \leftarrow \text{heat eq'n}$$