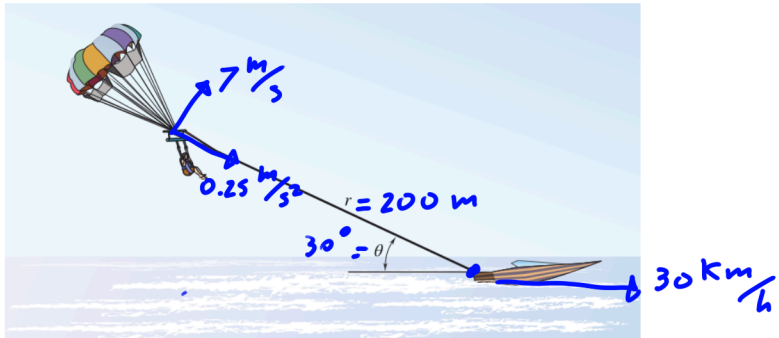


During a parasailing ride, the boat is traveling at a constant 30 km/hr with a 200-m long tow line. At the instant shown, the angle between the line and the water is 30° and is increasing at a constant rate of $2^\circ/s$. Determine the velocity and acceleration of the parasailer at this instant.



$$r = 200 \text{ m} \quad \frac{dr}{dt} = 0 \quad \frac{d^2r}{dt^2} = 0$$

$$\theta = 30^\circ \left(\frac{\pi \text{ rad}}{180^\circ} \right) \frac{d\theta}{dt} = 2 \frac{^\circ}{s} \left(\frac{\pi \text{ rad}}{180^\circ} \right) \frac{d^2\theta}{dt^2} = 0$$

$$= 0.52 \text{ rad} \quad = 0.035 \text{ rad/s}$$

$$\vec{V} = \frac{dr}{dt} \vec{e}_r + r \frac{d\theta}{dt} \vec{e}_\theta$$

$$= 0 \vec{e}_r + 200 \text{ m} \cdot 0.035 \text{ rad/s} \vec{e}_\theta = 7 \text{ m/s} \vec{e}_\theta$$

$$\vec{a} = \left(\frac{d^2r}{dt^2} - r \left(\frac{d\theta}{dt} \right)^2 \right) \vec{e}_r + \left(r \frac{d^2\theta}{dt^2} + 2 \frac{dr}{dt} \frac{d\theta}{dt} \right) \vec{e}_\theta$$

$$= 200 \text{ m} (0.035 \text{ rad/s})^2 \vec{e}_r + (200 \text{ m} \cdot 0 + 2 \cdot 0 \cdot 0.035 \text{ rad/s}) \vec{e}_\theta$$

$$= 0.25 \text{ m/s}^2 \vec{e}_r$$

$$30 \frac{\text{km}}{\text{h}} \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \left(\frac{1 \text{ h}}{3600 \text{ s}} \right) = 8.33 \text{ m/s}$$

$$\vec{V}_B = 8.33 \text{ m/s} \hat{i}$$

$$\vec{V}_P = 7 \text{ m/s} \vec{e}_\theta \quad \vec{e}_\theta = \sin 30 \hat{i} + \cos 30 \hat{j}$$

$$= 7 \text{ m/s} (0.5 \hat{i} + 0.87 \hat{j}) = 0.5 \hat{i} + 0.87 \hat{j}$$

$$= 3.5 \hat{i} + 6.1 \hat{j} \text{ m/s}$$

$$\vec{V} = \vec{V}_B + \vec{V}_P$$

$$= 8.33 \hat{i} + 3.5 \hat{i} + 6.1 \hat{j} \text{ m/s}$$

$$= 11.8 \hat{i} + 6.1 \hat{j} \text{ m/s}$$