

## freq.nybode Stability, GM, and PM from Bode plots

Bode plots are an alternative representation of the positive  $j\omega$ -axis Nyquist plot. As we established in [Lec. freq.nystab](#), this is sufficient information for stability via the Nyquist criterion. In a similar fashion, the gain and phase margins can also be found from the positive  $j\omega$ -axis Nyquist plot.

For these reasons, the stability, gain margin, and phase margin can all be found from the Bode plot. In fact, this is the preferred method for finding the gain and phase margins.

It is common, but somewhat risky, practice to simply use the Bode plot to determine stability, gain margin, and phase margin. Here is why it is risky: when we use it, we assume that the system

1. is open-loop stable;
2. with sufficient gain, has only clockwise encirclements of  $-1$ ; and
3. has a single negative-real-axis crossing.

Although these are all commonly met, there are plenty of systems for which they are not. For this reason, we encourage caution with this common practice. We proceed by describing the method.

Recall that the gain margin  $G_M$  is defined by the distance between the negative-real-axis intercept of a Nyquist plot and  $-1$ . This occurs at  $-180$  deg. On a Bode plot, such as that of [Fig. nybode.1](#), it is easy to determine the dB magnitude difference from the magnitude at  $-180$  deg and  $1 = 0$  dB.

Similarly, recall that the phase margin  $\Phi_M$  is defined as the difference between the angle at magnitude  $1 = 0$  dB and  $-180$  deg as the Nyquist plot approaches  $-180$  deg. On a Bode plot, such as that of [Fig. nybode.1](#), the magnitude  $0$  dB

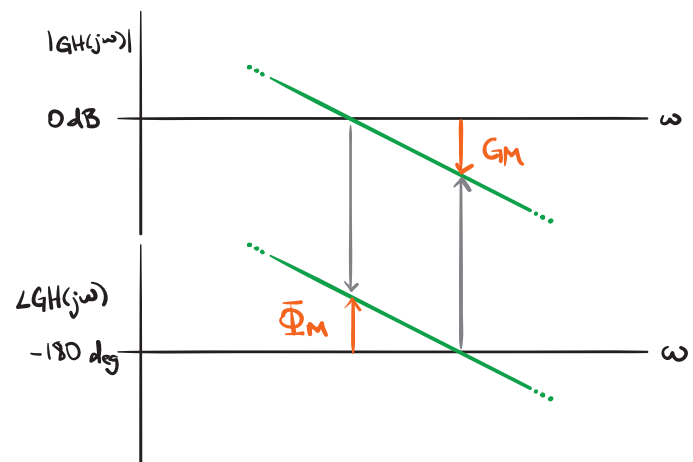


Figure nybode.1:

point near  $-180$  deg corresponds to the phase from which  $\Phi_M$  can be determined.

### Example freq.nybode-1

### re: Gain and phase margin from a Bode plot

Let the open-loop transfer function  $GH(s)$  be defined as

$$GH(s) = \frac{1}{s^3 + 2s^2 + 5s + 6}$$

Determine closed-loop stability, gain margin, and phase margin from an open-loop Bode plot.