ss.nt2ss Normal tree to state-space

- 1 At long last, we consider an algorithm to generate a state-space model from a linear graph model. In the following, we will consider a connected graph with E edges, of which S are sources (split between through-variable sources S_T and across S_A). There are 2E-S unknown across- and through-variables, so that's how many equations we need. We have E-S elemental equations and for the rest we will write continuity and compatibility equations. N is the number of nodes.
 - Derive 2E S independent differential and algebraic equations from elemental, continuity, and compatibility equations.
 - a) Draw a normal tree.
 - b) Identify primary and secondary variables.
 - c) Select the state variables to be across-variables on A-type branches and through-variables on T-type links.
 - d) Define the state vector **x**, input vector **u**, and output vector **y**.
 - e) Write an elemental equation for each passive element.⁴
 - f) Write a continuity equation for each passive branch by drawing a contour intersecting that and no other branch. Solve each for the secondary through-variable associated with that branch.⁵
 - g) Write a compatibility equation for each passive link by temporarily "including" it in the tree and finding the compatibility equation for the resulting loop. Solve each for the secondary across-variable associated with that link.⁶

normal tree

primary variables secondary variables

state variables

state vector input vector output vector elemental equation

4. There will be E - S elemental equations.

continuity equation

5. There will be $N-1-S_{\mathsf{A}}$ independent continuity equations.

compatibility equation

6. There will be $E-N+1-S_{\mathsf{T}}$ independent compatibility equations.

- 2. Eliminate variables that are not state or input variables and their derivatives. The following procedure is recommended.
 - a) Eliminate all secondary variables by substitution into the elemental equations of the continuity and compatibility equations.
 - b) Reduce the resulting set of equations to n (system order) in state and input variables, only. If not elimination, use linear algebra.
 - c) Write the result in standard form (Equation 1a or Equation 2a).
 - d) Express the output variables in terms of state and input variables, using any of the elemental, continuity, or compatibility equations.
 - e) Write the result in standard form (Equation 1b or Equation 2b).

Example ss.nt2ss-1

electronic the For system shown, find a state-space model with outputs i_L , I_s , and v_{R_2} .

re: circuit state-space model

