Iti.exe Exercises for Chapter Iti

Exercise Iti.oil

A certain sensor used to measure displacement ---/10 p. over time t is tested several times with input displacement $u_1(t)$ and a certain function $y_1(t)$ is estimated to properly characterize the corresponding voltage output. Assuming the sensor is linear and time-invariant, what would we expect the output sensor voltage $y_2(t)$ to be when the following input is applied?

$$u_2(t) = 3 \, \dot{u}_1(t) - 5 \, u_1(t) + \int_0^t 6 \, u_1(\tau) \, \mathrm{d}\tau \qquad (1)$$

Exercise Iti.water

A system with input u(t) and output y(t) has _____/15 p. the governing dynamical equation

 $2\ddot{y} + 12\dot{y} + 50y = -10\dot{u} + 4u.$ (2)

- a. What is the equilibrium y(t) when u(t) = 6?
- b. Demonstrate the stability, marginal stability, or instability of the system.

trans

Qualities of transient response

1 In this chapter, we explore the qualities of transient response—the response of the system in the interval during which initial conditions dominate.

We focus on characterizing first- and 2 second-order linear systems; not because they're easiest (they are), but because nonlinear systems can be linearized about an operating point and because higher-order linear system responses are just sums of first- and second-order responses, making "everything look first- and second-order." Well, many things, at least. 3 In this chapter, we primarily consider systems represented by single-input, single-output (SISO) ordinary differential equations (also called io ODEs)-with variable y representing the output, dependent variable time t, variable u representing the input, forcing function f, constant coefficients a_i, b_j , order n, and $\mathfrak{m} \leqslant \mathfrak{n}$ for $\mathfrak{n} \in \mathbb{N}_0$ —of the form

$$\frac{d^{n}y}{dt^{n}} + a_{n-1}\frac{d^{n-1}y}{dt^{n-1}} + \dots + a_{1}\frac{dy}{dt} + a_{0}y = f, \text{ where}$$
(1a)
$$f \equiv b_{m}\frac{d^{m}u}{dt^{m}} + b_{m-1}\frac{d^{m-1}u}{dt^{m-1}} + \dots + b_{1}\frac{du}{dt} + b_{0}u.$$
(1b)

Note that the forcing function f is related to but distinct from the input u. This terminology proves rather important.

linearization operating point

SISO

forcing function