## imp.divide The divider method

1 In Electronics, we developed the useful voltage divider formula for quickly analyzing how voltage divides among series electronic impedances. This can be considered a special case of a more general across-variable divider equation for any elements described by an impedance. After developing the across-variable divider, we also introduce the through-variable divider, which divides an input through-variable among parallel elements.

## Across-variable dividers

2 First, we develop the solution for the two-element across-variable divider shown in Figure divide.1. We choose the across-variable across  $Z_2$  as the output. The analysis follows the impedance method of Lecture imp.tf, solving for  $V_2$ .

- 1. Derive four independent equations.
  - a) The normal tree is chosen to consist of  $V_{in}$  and  $Z_2$ .
  - b) The elemental equations are
  - c) The continuity equation is
  - d) The compatibility equation is
- 2. Solve for the output  $V_2$ . From the elemental equation for  $Z_2$ ,

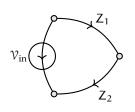


Figure divide.1: the two-element across-variable divider.

across-variable divider

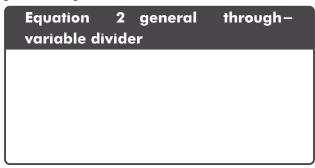
$$\begin{aligned} \mathcal{V}_2 &= \mathcal{F}_{\infty} Z_2 \\ &= \frac{\mathcal{V}_1}{Z_1} Z_2 \\ &= \frac{Z_2}{Z_1} (\mathcal{V}_{in} - \mathcal{V}_2) \quad \Rightarrow \\ \mathcal{V}_2 &= \frac{Z_2}{Z_1 + Z_2} \mathcal{V}_{in}. \end{aligned}$$

3 A similar analysis can be conducted for n impedance elements.

Equation variable div	 across–

Through-variable dividers

4 By a similar process, we can analyze a network that divides a through-variable into n parallel impedance elements.



Transfer functions using dividers

5 An excellent shortcut to deriving a transfer function is to use the across- and through-variable divider rules instead of solving the system of algebraic equations, as in Lec. imp.tf. An algorithm for this process is as follows.

- Identify the element associated with an output variable Y<sub>i</sub>. Call it the output element.
- Identify the source associated with an input variable U<sub>j</sub>. Set all other sources to zero.
- Transform the network to be an across- or through-variable divider that includes the "bare" (uncombined) output element's output variable.<sup>6</sup>
  - a) If necessary, form equivalent impedances of portions of the network, being sure to leave the output element's output variable alone.
  - b) If necessary, transform the source à la Norton or Thévenin.
- 4. Apply the across- or through-variable divider equation.
- 5. If necessary, use the elemental equation of the output element to trade output acrossand through-variables.
- 6. If necessary, use the source transformation equation of the input to trade input acrossand through-variables.
- 7. Divide both sides by the input variable.

6 It turns out that, despite its many "if necessary" clauses, very often this "shortcut" is easier than the method of Lecture imp.tf for low-order systems if only a few transfer functions are of interest. 6. In other words, if the across-variable of the output element is the output, do not combine it in series; if the through-variable is the output, do not combine it in parallel.

## Example imp.divide-1

## re: a circuit transfer function using a divider

Given the circuit shown with voltage source  $V_s$  and output  $v_L$ ,

