

fun.vdiv Voltage dividers

In [Chapter can](#) we'll learn about how to approach circuit analysis in a systematic way. For now, we'll limp along unsystematically with our toolbelt of concepts and equations in order to introduce some more circuit elements, concepts, and theorems. But we can't resist just a bit of circuit analysis now.

The voltage divider is a ubiquitous and useful circuit. In a sense, it's less of a circuit and more of a concept. For resistors, that concept can be stated as the following.

voltage divider

The voltage across resistors in series is divided among the resistors.

An immediately useful result is that we can "divide voltage" into any smaller voltage we like by putting in a couple resistors.

In order to show how the voltage divider "divides up" the voltage, we must do some basic circuit analysis. Consider the circuit in [Fig. vdiv.1](#). The input voltage v_{in} is divided into v_{R_1} and $v_{R_2} = v_{out}$. We want to know v_{out} as a function of v_{in} and parameters R_1 and R_2 . Let's write down the equations we know from the laws of Kirchhoff and Ohm:

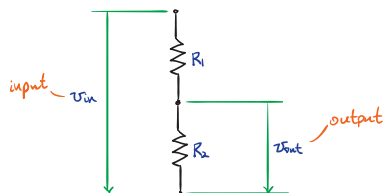


Figure vdiv.1: a simple voltage divider circuit.

We've already established that $v_{out} = v_{R_2}$, so we can solve for v_{R_2} in (*). We want to eliminate the three "unknown" variables v_{R_1} , i_{R_1} , and i_{R_2} , so it is good that we have four equations.³ We begin with (*b) and proceed by substitution of the others of (*):

3. Alternatively, we could solve for all four unknown variables with our four equations.



Nice! So we can now write the input-output relationship for a two-resistor voltage divider.

Equation 1 two-resistor voltage divider

So the voltage divider had the effect of dividing the input voltage into a fraction governed by the relationship between the relative resistances of the two resistors. This fraction takes values in the interval $[0, 1]$. Now, whenever we see the voltage divider circuit, we can just remember this easy formula!

Similarly, for n resistors in series, it can be shown that the voltage divider relationship is as follows.

Equation 2 general voltage divider

A large, empty rectangular box with a thin black border, intended for the user to write the equation for a general voltage divider.