## sets.exe Exercises for Chapter sets

Exercise sets.hardhat

For the following, write the set described in set-builder notation.

- a.  $A = \{2, 3, 5, 9, 17, 33, \dots \}.$
- b. B is the set of integers divisible by 11.
- c.  $C = \{1/3, 1/4, 1/5, \cdots\}.$
- d. D is the set of reals between -3 and 42.

Exercise sets.2

Let  $x, y \in \mathbb{R}^n$ . Prove the Cauchy-Schwarz Inequality

$$|\mathbf{x} \cdot \mathbf{y}| \leq \|\mathbf{x}\| \|\mathbf{y}\|. \tag{1}$$

Hint: you may find the geometric definition of the dot product helpful.

Exercise sets.3

Let  $\mathbf{x} \in \mathbb{R}^n$ . Prove that

$$\mathbf{x} \cdot \mathbf{x} = \|\mathbf{x}\|^2. \tag{2}$$

Hint: you may find the geometric definition of the dot product helpful.

Exercise sets.4

Let  $x, y \in \mathbb{R}^n$ . Prove the Triangle Inequality

$$\|\mathbf{x} + \mathbf{y}\| \le \|\mathbf{x}\| + \|\mathbf{y}\|.$$
 (3)

Hint: you may find the Cauchy-Schwarz Inequality helpful.

## prob

## **Probability**